



# Calculations

Electrical

Aluminum Bus Bar Calculation

Titanium Sponge Plant

RTI International Metals, Inc.

Hamilton, Monroe County, MS

Job Number: 444345

Revision	Date	Originator	Checker	Approved
0	7/28/08	Bahram Zamani	HA/JF	<i>Jim Fuller</i>



Aluminum Bus Bar Calculations  
Titanium Sponge Plant  
Job Number: 444345

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### **1.0 Objective:**

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Calculate the size of the aluminum bus bar used to supply DC power to Titanium Cells inside Area 300.

### **2.0 Assumptions:**

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- The 40 magnesium electrolysis cells require 6VDC for each cell. The bus shall deliver total of 86,000 amperes at 240VDC.
- Aluminum bus bar is chosen for cost saving
- The ambient temperature is 40 deg C at the Mg Recovery Area 300 which is cooled by (16) 30 hp fans incorporated in the walls of the building
- Maximum operating temperature for aluminum bus bar is 90 deg C, recommended by manufacturer.
- If the bus bars be closer than 7-7/8" together then the heat will increase and consequently the resistance of the bus bar and the voltage drop will increase causing problems for the cells.

### **3.0 Design Basis/Criteria and References:**

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Calculate the size of the aluminum bus bar used to supply DC power to Titanium Cells inside Area 300. The aluminum bus bar shall sufficiently large to carry 85000 amps thru 240VDC system. The alum. Bus bar should not be over 90deg C.



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#### 4.0 Results and Conclusions:

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##### Calculations:

Attachment A: Calculation performed by Abe with Neeltran Co. dated 12/13/07. Results indicate two 8"x32" aluminum bus bars separated 7-7/8" apart at 40 deg C ambient temperature, carrying 85,000 amperes. The bus temperature reaches to 91deg C for normal air convection and 85 deg C for normal air convection together with normal heat radiating from bus.

Attachment B: Calculation performed by Andrew Fynan with Sidehill Copper Works, Inc. dated 11/29/07. Results indicate two 7.87"x 31.5" aluminum bus bars separated 7.87" apart at 40 deg C ambient temperature carrying 86,000 amps. The bus temperature reaches to 83 deg C for normal air convection together with normal heat radiating from bus.

Attachment C: In-house manual calculation. Results indicate two 7.87"x 32" aluminum bus bars separated 7.87" apart, at 40 deg C ambient temperature with 50 deg C rise results in 85,539 amps bus. Also the voltage drop for the entire length of 1250 feet of bus bar is 2.42 Volts on the 240VDC system.

Attachment D: This calculation is for the aluminum bus bar in the rectifier area. Two 5"x 20" aluminum bus bars separated 5" apart at 40 deg C ambient with 50 deg rise results in 44,915 amps for one rectifier bus bar.

##### Results

Parsons choose two 7-7/8 " x 32" aluminum bus bars separated 7-7/8" apart, based on ampere and heat dissipation from two manufacturer's calculations.

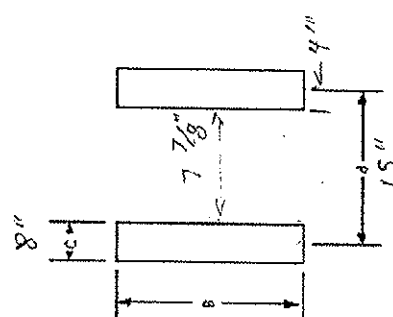
ALUM BUS  
BAR CALC  
BY NEELTRAN

# Parallel Rectangular Bus Bar Design

Rev: 12/13/2007

= Aluminum

Single Water Cooled BUSSBAR @ desired temperature	Losses in Watts	Bus Temp. °C for convection only	Bus Temp. °C convection & radiation
	725708	91	
Natural convection total bus	362839	91	85
Radiated heat loss, W	16766		
Nominal Current in A	85000	0	Hz
AC Current Phase Angel in degrees: (positive for current lagging voltage, negative for leading)	0	Enter 1 for single phase and 3 for three phase	1
Nominal Voltage in Volts	240		
BUS Ambient Temp. in °C	40	Desired Bus °C	91
ENTER EVEN NUMBER OF EQUALLY SPACED BUS BARS HERE:			
Fan Factor (1 for natural convection, higher for forced air)			2
Estimated airflow on busbars, Linear Foot per minute			1
			229



1 Pair(s) of Equally-spaced Busbars as:

BUS MATERIAL, CU or AL	AL
Total BUS Inductance in µH	596.00
Individual bar resistance at desired bus temperature in µΩ	100.44
Current carrying skin thickness in inch (two sides)	8.00
Total Bus resistance, µΩ per linear foot	0.033
Volt-drop at nominal current per foot	0.0028

l is the length of buss bars

B, in/cm	C, in/cm	d, in/cm	l, in/cm
32.000	8.000	15.748	18000.000
81.280	20.320	40.000	45720.000

CU temp coeff	0.00393	ε 1/deg K
AL temp coeff	0.00430	
CU density, lb/in <sup>3</sup>	0.321	
AL density, lb/in <sup>3</sup>	0.098	

Total Weight of Bus, lb	451584
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**Zamani, Bahram**

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**From:** ABE [abe@neeltran.com]  
**Sent:** Thursday, December 13, 2007 9:46 AM  
**To:** Zamani, Bahram  
**Cc:** dmaguire@rtiintl.com; Tony  
**Subject:** re: Bus Bar sizing  
**Attachments:** Bus Bar Thermal 121307 natural 40C.pdf

Hi Bahram,

Per your request, I have attached estimated thermal for the 8"x32" Aluminum busbar with and without the effect of radiation. I assumed only natural convection with no fan air blowing. In reality, the fans will make a substantial reduction on temperature rise. Even with no fan, the temperature rise looks acceptable when I subtracted the radiated heat losses.

Hope this data helps you finalize your design.

Regards,  
Abe

| On Tuesday, December 11, 2007 12:00 PM, ABE wrote:

**Date:** Tue, 11 Dec 2007 12:00:11 -0500  
**From:** ABE  
**To:** "Zamani, Bahram"  
**Subject:** re: Bus Bar sizing

\*\*\* Attachment omitted: BUS BAR THERMAL 121107 FAN 50C.PDF  
\*\*\* Attachment omitted: BUS BAR THERMAL 121107 NATURAL 40C.PDF  
\*\*\* Attachment omitted: BUS BAR THERMAL 121107 NATURAL 50C.PDF

Hi Bahram,

I ran my Busbar design program for your busbar under three conditions:

1. Naturally convected at 40 deg C ambient (narrowly unacceptable at 94 deg C)
2. Naturally convected at 50 deg C ambient (unacceptable at 107 deg C)
3. Forced convected at 50 deg C ambient (acceptable at 77 deg C)

Please note to air speed data as an estimate for fan air flow requirements. In forced fan air flow, air speed is by the fan. In natural convection, air speed is a function of the temperature difference of the busbar and ambient. Please also note to the margin of error as there are other physical factors that may influence the simulation results.

Regards,  
Abe

| On Monday, December 10, 2007 1:42 PM, Zamani, Bahram wrote:

Sidehill Copper Works, Inc.  
Preliminary Conductor Sizing

**PROPRIETARY**

Date November 30, 2007  
Customer Parsons

mm	inches
200	7.874
800	31.496

Operating Current I1	86000 (amps)
Number of bars n	2
thickness of bars t	7.874 (in) ✓
width of bars h	31.496 (in) ✓
gap between bars g	7.874 (in) ✓
Atmospheric pressure p	1 (atmospheres)
conductivity z	59 (% IACS)
Ambient temp deg C t1	50 (deg C)
operating temp deg C t2	83 (deg C)
Ambient temp deg K T1	323.15 (deg K)
operating Temp deg K T2	356.15 (deg K)
Temp rise deg C Dt	33
alpha a	0.004
Total cross section Aa	496.00 (sq in)
current density	173.39 (amps/sq in)

gap emmissivity ei = 0.9  
bar emmissivity eo = 0.5

current rating at Top I2 87557.267 (amps)

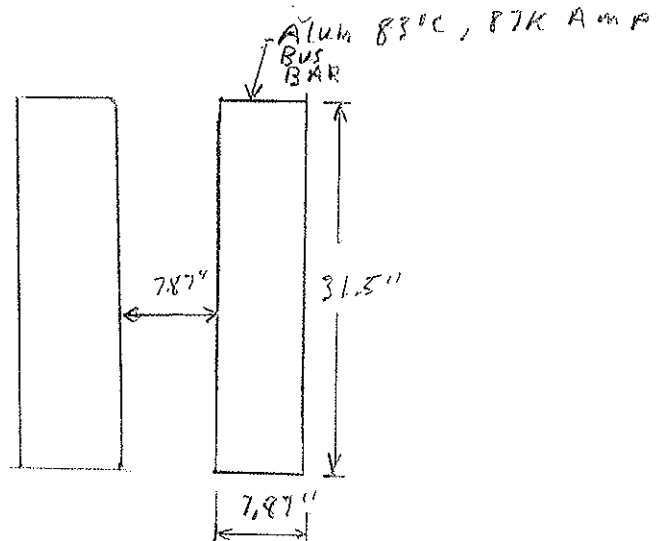
583.29 lb. per ft.

Area convective inner Aci	755.90 (sq in / ft)
Area convective outer Aco	1133.86 (sq in / Ft)
Area radiative inner Ari	188.98 (sq in / ft)
Area Radiative outer Aro	1133.86 (sq in / ft)

resist. @ 20 deg C R20	2.784E-08 (ohms / ft)
resist. @ Top Rt	3.485E-08 (ohms / ft)

Convect. Loss WcAc = 126.18718 (WATTS /FT)  
Radiative Loss WrAr = 140.99059 (WATTS /FT)  
Power Loss at T op = 267.17776 (WATTS /FT)  
Voltage drop at T op = 0.0031067 (VOLTS/FT)

current rating at Top I2 87557 (amps) ←



**Zamani, Bahram**

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**From:** Andrew Fynan [afynan@sidehillcopper.com]  
**Sent:** Thursday, November 29, 2007 11:57 AM  
**To:** Zamani, Bahram  
**Subject:** Re: Bus Bar design

Bahram

There aren't very many places left casting heavy high conductivity aluminum sections so I don't know if 7" x 30" size is still cast.

2 bars 7" x 30" for 86,000 amps estimated 41 deg C rise @ .004 V /ft

The closest I can come from my metal source is a little bigger

2 bars 200mm x 800mm AA1370 (7.87" x 31.50") 33 deg C rise .003 V/ft (not bad)

If there is field temp rise and voltage drop data from the prior installation that would be useful as the above values are estimates in free air.

Do you have drawing M-019 ? That looks like it would show the flexibles between the bus and the anodes - are they in the bus scope?

I'm assuming anode is upper furnace connection - is this correct?

Lower connection to furnace- is this a rigid bus connection or is it also flexible?

It looks like the bus could be mostly shop fabricated - making upper bus of one cell to lower bus overall length around

When you have a moment please call.

Best Regards,

Andrew Fynan  
Sidehill Copper Works, Inc.  
12 Port Access Rd.  
Erie, PA 16507  
[www.sidehillcopper.com](http://www.sidehillcopper.com)  
[afynan@sidehillcopper.com](mailto:afynan@sidehillcopper.com)

----- Original Message -----

**From:** [Zamani, Bahram](mailto:Zamani, Bahram)  
**To:** [afynan@sidehillcopper.com](mailto:afynan@sidehillcopper.com)  
**Sent:** Thursday, November 29, 2007 11:51 AM  
**Subject:** Bus Bar design

Hi Andrew,

Attached please see the partial floor plan of new design and the typical incoming cell bus bar arrangement details. Please be informed that the details has been copied from the old plan documents and have to be modified for the new design. As you may seen (2) 7" X 30" BARS WITH 19" spacing in between have been used for 60 similar cells with total of 3747line ft. I wonder if we can go with same since in the new plan we only 40 cells with 1500 line ft, please advise.

2/12/2008

**Zamani, Bahram**

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**From:** Andrew Fynan [afynan@sidehillcopper.com]  
**Sent:** Friday, November 30, 2007 11:56 AM  
**To:** Zamani, Bahram  
**Subject:** Re: Buss Bar sizing  
**Attachments:** PARSONS PRELIMINARY SIZING Sidehill.pdf

Please see attached  
Best Regards,

Andrew Fynan  
Sidehill Copper Works, Inc.  
12 Port Access Rd.  
Erie, PA 16507  
[www.sidehillcopper.com](http://www.sidehillcopper.com)  
[afynan@sidehillcopper.com](mailto:afynan@sidehillcopper.com)

----- Original Message -----

**From:** Zamani, Bahram  
**To:** [afynan@sidehillcopper.com](mailto:afynan@sidehillcopper.com)  
**Sent:** Friday, November 30, 2007 10:17 AM  
**Subject:** Buss Bar sizing

Hi Andrew,  
Attached please find "out going cell bus bar detail shown on drawing M-45" and also drawing M-19. Please give a call if any question.

<b>PARSONS</b>		Job Number	WBS Number	Page Number	Sheet 10 5
Calculation Sheet		443821	—	5	

Rev	Date	By	Ck	Title
A	2/25/08	BZ	AH	DC BUS BAR CALCULATION RTE TITANIUM PROJECT

$$I_{(AMP)} = \frac{A^{0.5} \times P^{0.39} \times \theta^{0.61}}{[(1 + \alpha \theta) \rho]^{0.5}} \times (1.02)$$

A = CROSS-SECTION AREA, mm<sup>2</sup>

P = PERIMETER OF CONDUCTOR, mm

θ = TEMPERATURE DIFFERENCE BETWEEN CONDUCTOR AND AMBIENT TEMP., C°

α = RESISTANCE TEMPERATURE COEFFICIENT OF ALUMINUM AT AMBIENT TEMP. PER C°

ρ = RESISTIVITY OF ALUMINUM, Ω cm

GIVEN:

$$\text{BAR} \Rightarrow 7\frac{7}{8}'' \times 32''$$

$$1'' = 25.4 \text{ mm}$$

$$\text{BAR} \Rightarrow 200.025 \text{ mm} \times 812.8 \text{ mm}$$

$$A = 200.025 \times 812.8 = 162580 \text{ mm}^2$$

$$P = (200.025 + 812.8) \times 2 = 2025.65 \text{ mm}$$

$$\alpha = 0.004 \text{ C}^\circ$$

$$\theta = 90^\circ \text{C} - 40^\circ \text{C} = 50^\circ \text{C}$$

$$\rho = 2.81 \mu\Omega \text{ cm (FOR ALUMINUM AA 1350)}$$

<b>PARSONS</b>		Job Number	WBS Number	Page Number	Sheet 2 of 5
Calculation Sheet					

Rev	Date	By	Ck	Title
A	2/15/08			DC BUS BAR CALCULATIONS RTI Titanium Project

$$I_{\text{Camp}} = \frac{\left[ (162520)^{0.5} \times (2025.65)^{0.39} \times 50^{0.61} \right] \times 1.02}{\left[ (1 + 0.004 \times 50)(2.8) \right]^{0.5}}$$

$$I = \frac{87109.5}{1.833} = 47,522 \text{ AMP}$$

$$\text{TOTAL RATING} = I \times (\text{LAMINATION'S MULTIPLYING FACTOR})$$

$$= I \times 1.8 \text{ (FOR 2 BARS)}$$

$$= \boxed{85539.8 \text{ AMP}}$$

54 30FS



Reference

Aluminum Alloy AA 1350

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Wrought:  
AA 1xxx  
AA 2xxx  
AA 3xxx  
AA 4xxx  
AA 5xxx  
AA 6xxx  
AA 7xxx  
Cast:  
2xx.0 or x2xx.0  
3xx.0 or x3xx.0  
4xx.0 or x4xx.0  
5xx.0 or x5xx.0  
7xx.0  
8xx.0
- **Specific Al Alloy**  
General Information
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Bibliography

**AA 1350**

**Category** Aluminum Alloy  
**Class** Wrought

**Composition**

Element	Weight %
Al	99.50 (min)

**Mechanical Properties**

Properties	Conditions	
	T (°C)	Treatment
<b>Density</b> (×1000 kg/m <sup>3</sup> )	2.6-2.8	25
<b>Poisson's Ratio</b>	0.33	25
<b>Elastic Modulus</b> (GPa)	70-80	25
<b>Tensile Strength</b> (Mpa)	97	
<b>Yield Strength</b> (Mpa)	83	
<b>Elongation</b> (%)	25	H12 <a href="#">more</a>
<b>Reduction in Area</b> (%)		
<b>Shear Strength</b> (MPa)	62	25 H12 <a href="#">more</a>
<b>Fatigue Strength</b> (MPa)	48	25 H19

**Thermal Properties**

Properties	Conditions	
	T (°C)	Treatment
<b>Thermal Conductivity</b> (W/m-K)	230	25 All H1x <a href="#">more</a>

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SA 4015

## Electric Properties

Properties	Conditions	
	T (°C)	Treatment
<b>Electric Resistivity</b> ( $10^{-9}\Omega\text{-m}$ )	28	Hlx <a href="#">more</a>

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Calculation Sheet

5 of 5

Rev	Date	By	Ck	Title
A	2-27-08	BZ	HA	DC BUS BAR VOLTAGE DROP CALCULATION 240VDC BUS

$$R = \rho \frac{L}{A \times 2 \text{ (2 BARS)}}$$

L = LENGTH OF THE BAR cm.

R = RESISTANCE  $\Omega$  cm

A = CROSS-SECTION AREA  $cm^2$

$\rho$  = RESISTIVITY OF ALUMINUM  $\Omega$  cm

$$L = 1250 \text{ ft} \times 30.48 \frac{cm}{ft} = 38100 \text{ cm}$$

$$A = (32 \text{ "} \times 25.4 \text{ cm}) \times (7.275 \text{ "} \times 25.4 \text{ cm}) = 1626 \text{ cm}^2$$

$$R = 2.8 \times 10^{-6} \times \frac{38100 \text{ cm}}{2 \times 1626 \text{ cm}^2} = 2.82 \times 10^{-5} \Omega$$

$$V = R I$$

$$= 2.82 \times 10^{-5} \times 86000 \text{ Ampere} = 2.42 \text{ V}_{drop} \text{ OR } 0.019 \text{ V PER ft}$$

<b>PARSONS</b>				Job Number	WBS Number	Page Number	Sheet of
Calculation Sheet							1 of 1

Rev	Date	By	Ck	Title
A	2/27/08	BZ	HA	DC BUS BAR CALCULATION 5" x 20" ⇒ 127mm x 508mm

$$I = \frac{A^{0.5} \times P^{0.039} \times \theta^{0.61}}{[(1 + \alpha \theta) P]^{0.5}} \times (1.02)$$

$$A = (5'' \times 25.4) \times (20'' \times 25.4) = 127\text{mm} \times 508\text{mm}$$

$$P = [(5'' \times 25.4) + (20'' \times 25.4)] \times 2 = 1270$$

$$I = \frac{(64516)^{0.5} \times (1270)^{0.039} \times (50)^{0.61}}{[(1 + 0.004 \times 50) \cdot 2.8]^{0.5}} \times 1.02$$

$$= \frac{45739}{1.833} = 24953 \text{ AMP}$$

$$I_{\text{TOTAL}} = (1.8) \times 24953 = 44915 \text{ AMP} \quad \text{meets the required } 43,000 \text{ A for each Rectifier}$$